Deriving Via

or, How to Turn Hand-Written Instances into an Anti-Pattern

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Abstract

Haskell's deriving construct is a cheap and cheerful way to quickly generate instances of type classes that follow common patterns. But at present, there is only a subset of such type class patterns that deriving supports, and if a particular class lies outside of this subset, then one cannot derive it at all, with no alternative except for laboriously declaring the instances by hand.

To overcome this deficit, we introduce Deriving Via, an extension to deriving that enables programmers to compose instances from named programming patterns, thereby turning deriving into a high-level domain-specific language for defining instances. Deriving Via leverages newtypes—an already familiar tool of the Haskell trade—to declare recurring patterns in a way that both feels natural and allows a high degree of abstraction.

CCS Concepts • Software and its engineering \rightarrow Functional languages; *Data types and structures*;

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1 Introduction

In Haskell, type classes capture common interfaces. When defining class instances, we often discover repeated patterns where different instances have the same definition. For example, the following instances appear in the base library of the Glasgow Haskell Compiler (GHC):

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```
instance Monoid a => Monoid (IO a) where
  mempty = pure mempty
  mappend = liftA2 mappend
instance Monoid a => Monoid (ST s a) where
  mempty = pure mempty
  mappend = liftA2 mappend
```

These have completely identical instance bodies. The underlying pattern works not only for IO and ST s, but for any applicative functor f.

It is tempting to avoid this obvious repetition by defining an instance for all such types in one fell swoop:

```
instance (Applicative f, Monoid a)
  => Monoid (f a) where
  mempty = pure mempty
  mappend = liftA2 mappend
```

Unfortunately, this general instance is undesirable as it overlaps with all other (f a)-instances. Instance resolution will match the instance head first before considering the context, whether f is applicative or not. Once GHC has commited to an instance, it will never backtrack. Consider:

newtype Endo a = MkEndo (a -> a) - Data.Monoid

Here, Endo is not an applicative functor, but it still admits a perfectly valid Monoid instance that overlaps with the general instance above:

```
instance Monoid (Endo a) where
mempty = MkEndo id
mappend (MkEndo f) (MkEndo g) = MkEndo (f . g)
```

Moreover, even if we have an applicative functor f on our hands, there is no guarantee that this is the definition we want. Notably, lists are the *free monoid* (i.e, the most 'fundamental' monoid) but that instance does not coincide with the rule above and in particular, imposes no (Monoid a) constraint:

```
instance Monoid [a] where
  mempty = []
  mappend = (++)
```

In fact, the monoid instance for lists is captured by a *different* rule based on Alternative:

instance Alternative f => Monoid (f a) where mempty = empty mappend = (<|>)

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Because instance resolution never backtracks, we cannot define these two distinct rules for Monoid (f a) at the same time, even with overlapping instances.

The only viable workaround using the Haskell type class system is to write the instances for each data type by hand, each one with an identical definition (like the instances for IO a and ST s a), which is extremely unsatisfactory:

- It is not obvious that we are instantiating a general principle.
- Because the general principle is not written down in code with a name and documentation, it has to be communicated through folklore or in comments and is difficult to discover and search for. Our code has lost a connection to its origin.
- There are many such rules, some quite obvious, but others more surprising and easy to overlook.
- While the work required to define instances manually for Monoid—which only has two methods—is perhaps acceptable, it quickly becomes extremely tedious and error-prone for classes with many methods.

As an illustration of the final point, consider Num. There is a way to lift a Num instance through any applicative functor:¹

```
instance (Applicative f, Num a) => Num (f a) where
 (+) = liftA2 (+)
 (-) = liftA2 (-)
 (*) = liftA2 (*)
 negate = liftA negate
 abs = liftA abs
 signum = liftA signum
 fromInteger = pure . fromInteger
```

Defining such boilerplate instances manually for concrete type constructors is so annoying that Conal Elliott introduced a preprocessor [8] for this particular use case several years ago.

1.1 Deriving

Readers familiar with Haskell's deriving mechanism may wonder why we cannot simply derive all the instances we just discussed. Unfortunately, our options are very limited.

To start, Monoid is not one of the few blessed type classes that GHC has built-in support to derive. It so happens that (IO a), (ST s a) and (Endo a) are all newtypes, so they are in principle eligible for *generalized newtype deriving* (GND), in which their instances could be derived by reusing the instances of their underlying types [1]. However, this would give us the wrong definition in all three cases.

Our last hope is that the the Monoid type class has a suitable generic default implementation [11]. If that were the case, we could use a deriving clause in conjunction with the DeriveAnyClass extension, and thereby get the compiler to generate an instance for us.

However, there is no generic default for Monoid, a standard class from the base library (which would be difficult to change). But even if a generic instance existed, it would still capture a *single* rule over all others, so we couldn't ever use it to derive both the monoid instance for lists and that for ST s a.

We thus have no other choice but to write some instances by hand. This means that we have to provide explicit implementations of at least a minimal subset of the class methods. There is no middle ground here, and the additional work required compared to deriving can be drastic—especially if the class has many methods—so the option of using deriving remains an appealing alternative.

1.2 Introducing Deriving Via

We are now going to address this unfortunate lack of abstraction and try to bridge the gap between manually defined instances and the few available deriving mechanisms we have at our disposal.

Our approach has two parts:

- 1. We capture general rules for defining new instances using newtypes.
- 2. We introduce Deriving Via, a new language construct that allows us to use such newtypes to explain to the compiler exactly how to construct the instance without having to write it by hand.

As a result, we are no longer limited to a fixed set of predefined ways to define particular class instances, but can instead teach the compiler new rules for deriving instances, selecting the one we want using a high-level description.

Let us look at examples. For the *first part*, we revisit the rule that explains how to lift a monoid instance through an applicative functor. We can turn the problematic generic and overlapping instance for Monoid (f a) into an entirely unproblematic instance by defining a suitable adapter new-type [9] and wrapping the instance head in it:

```
newtype Ap f a = Ap (f a)
instance (Applicative f, Monoid a)
=> Monoid (Ap f a) where
mempty = Ap (pure mempty)
mappend (Ap f) (Ap g) = Ap (liftA2 mappend f g)
```

Since GHC 8.4, we also need a Semigroup instance, because it is now a superclass of Monoid²:

```
instance (Applicative f, Semigroup a)
  => Semigroup (Ap f a) where
  Ap f <> Ap g = Ap (liftA2 (<>) f g)
```

¹Similarly for Floating and Fractional, numeric type classes with a combined total of 25 methods (15 for a minimal definition).

²See Section 4.4 for a more detailed discussion of this aspect.

Deriving Via

The *second part* is to now use such a rule in our new form of deriving statement. We can do this when defining a new data type, such as in

```
data Maybe a = Nothing | Just a
    deriving Monoid via (Ap Maybe a)
```

This requires that we independently have an Applicative instance for Maybe, but then we obtain the desired Monoid instance nearly for free.

In the deriving clause, via is a new language construct that explains *how* GHC should derive the instance, namely by reusing the Monoid instance already available for the via type, Ap Maybe a. It should be easy to see why this works: due to the use of a newtype, Ap Maybe a has the same internal representation as Maybe a, and any instance available on one type can be made to work on the other by suitably wrapping or unwrapping a newtype. In more precise language, Ap Maybe a and Maybe a are representationally equal [1].

The Data.Monoid module defines many further adapters that can readily be used with Deriving Via. For example, the rule that obtains a Monoid instance from an Alternative instance is already available through the Alt newtype:

```
newtype Alt f a = Alt (f a)
```

```
instance Alternative f => Monoid (Alt f a) where
  mempty = Alt empty
  mappend (Alt f) (Alt g) = Alt (f <|> g)
instance Alternative f => Semigroup (Alt f a) where
  (<>) = mappend
```

Note that while Alt has the same definition as Ap, its Monoid instance is different, and by naming the type in a via clause, we can explicitly select the instance we are interested in.

Using adapters such as Ap and Alt, a vast amount of Monoid instances that currently have to be defined by hand can instead be derived using the via construct.

1.3 Contributions and Structure of the Paper

Many hand-written instances that occur in Haskell code are in fact instantiations of similar rules as we have just shown, and can be replaced by Deriving Via. We argue that expressing an instance as the instantiation of a rule should be the norm, and using a hand-written instance when a rule could be used instead should be discouraged, or even be considered an anti-pattern.

Throughout the paper, we provide many additional examples of the use of Deriving Via, starting with a case study using the QuickCheck library (Section 2).

We also provide a detailed explanation of how to typecheck and translate Deriving Via clauses (Section 3).

The idea of Deriving Via is surprisingly simple, yet it has a number of powerful and equally surprising properties:

• It further generalizes the *generalized newtype deriving* extension. (Section 3.2.1).

- It additionally generalizes the concept of *default signatures*. (Section 4.2).
- It provides a possible solution to the problem of introducing additional boilerplate code when introducing new superclasses (such as Applicative for Monad, Section 4.4).
- It allows for reusing instances not just between representationtally equal types, but also between isomorphic or similarly related types (Section 4.3).

Our extension is fully implemented in GHC and will be present in version 8.6.

2 Case Study: QuickCheck

QuickCheck [3] is a well-known Haskell library for randomized property-based testing. At the core of QuickCheck's test-case generation functionality is the Arbitrary class. Its primary method is arbitrary, which describes how to generate suitable random values of a given size and type. It also has a method shrink that is used to try to shrink failing counterexamples of test properties.

Many standard Haskell types, such as Int and lists, are already instances of Arbitrary. This can be very convenient, because many properties involving these types can be quickchecked without any extra work.

On the other hand, there are often additional constraints imposed on the actual values of a type that are not sufficiently expressed in their types. Depending on the context and the situation, we might want to guarantee that we generate positive integers, or non-empty lists, or even sorted lists.

The QuickCheck library provides a number of newtypebased adapters (called *modifiers* in the library) for this purpose. As an example, QuickCheck defines:

```
newtype NonNegative a =
NonNegative {getNonNegative :: a}
```

which comes with a predefined instance of the form

```
instance (Num a, Ord a, Arbitrary a)
=> Arbitrary (NonNegative a)
```

that explains how to generate and shrink non-negative numbers. A user who wants a non-negative integer can now use NonNegative Int rather than Int to make this obvious.

This approach, however, has a drastic disadvantage: we have to wrap each value in an extra constructor, and the newtype and constructor are QuickCheck-specific. An implementation detail (the choice of testing library) leaks into the data model of an application. While we might be willing to use domain-specific newtypes for added type safety, such as Age or Duration, we might not be eager to add QuickCheck modifiers everywhere. And what if we need more than one modifier? And what if other libraries export their own set of modifiers as well? We certainly do not want to change the actual definition of our data types (and corresponding code) whenever we start using a new library.

With Deriving Via, we have the option to reuse the existing infrastructure of modifiers without paying the price of cluttering up our data type definitions. We can choose an actual domain-specific newtype such as

newtype Duration = Duration Int - in seconds

and now specify exactly how the Arbitrary should be derived for this:

deriving Arbitrary via (NonNegative Int)

This yields an Arbitrary instance that generates only nonnegative integers. Only the deriving clause changes, not the data type itself. If we later decide we want only positive integers as durations, we replace NonNegative with Positive in the deriving clause. Again, the data type itself is unaffected. In particular, we do not have to change any constructor names anywhere in our code.

2.1 Composition

Multiple modifiers can be combined. For example, there is another modifier called Large that will scale up the size of integral values being produced by a generator. It is defined as

newtype Large a = Large {getLarge :: a}

with a corresponding Arbitrary instance:

instance (Integral a, Bounded a) => Arbitrary (Large a)

For our Duration type, we can easily write³

deriving Arbitrary via (NonNegative (Large Int))

and derive an instance which only generates Duration values that are both non-negative *and* large. This works because Duration still shares the same runtime representation as NonNegative (Large Int) (namely, that of Int), so the latter's Arbitrary instance can be reused.

2.2 Adding New Modifiers

Of course, we can add add our own modifiers if the set of predefined modifiers is not sufficient. For example, it is difficult to provide a completely generic Arbitrary instance that works for all data types, simply because there are too many assumptions about what makes good test data that need to be taken into account.

But for certain groups of data types, there are quite reasonable strategies of coming up with generic instances. For example, for enumeration types, one strategy is to desire a uniform distribution of the finite set of values. QuickCheck even offers such a generator, but it does not expose it as a newtype modifier: arbitraryBoundedEnum :: (Bounded a, Enum a) => Gen a

But from this, we can easily define our own:

```
newtype BoundedEnum a = BoundedEnum a
instance (Bounded a, Enum a)
=> Arbitrary (BoundedEnum a) where
arbitrary = BoundedEnum <$> arbitraryBoundedEnum
```

We can then use this functionality to derive Arbitrary for a new enumeration type:

```
data Weekday = Mo | Tu | We | Th | Fr | Sa | Su
  deriving (Enum, Bounded)
  deriving Arbitrary via (BoundedEnum Weekday)
```

2.3 Parameterized Modifiers

Sometimes, we might want to parameterize a generator with extra data. We can do so by defining a modifier that has extra arguments and using those extra arguments in the associated Arbitrary instance.

An extreme case that also makes use of type-level programming features in GHC is a modifier that allows us to specify a lower and an upper bound of a generated natural number.

```
newtype Between (1 :: Nat) (u :: Nat) = Between Integer
instance (KnownNat 1, KnownNat u)
=> Arbitrary (Between 1 u) where
arbitrary = Between <$>
choose (natVal @l Proxy, natVal @u Proxy)
```

(Note that this instance makes use of visible type application [7] in natVal @l and natVal @u.)

We can then equip an application-specific type for years with a generator that lies within a plausible range:

```
newtype Year = Year Integer
deriving Show
deriving Arbitrary via (Between 1900 2100)
```

In general, we can use this technique of adding extra parameters to a newtype to support additional ways to configure the behavior of derived instances.

3 Typechecking and Translation

Seeing enough examples of Deriving Via can give the impression that it is a somewhat magical feature. In this section, we aim to explain the magic underlying Deriving Via by giving a more precise description of:

- how Deriving Via clauses are typechecked,
- what sort of code Deriving Via generates behind the scenes, and
- how to determine the scoping of type variables in Deriving Via clauses.

³Here and in many later places, we use deriving clauses in isolation, in order to highlight the part of the syntax we are focusing on and to not repeat data or newtype unnecessarily often. It is still understood that the deriving clause is syntactically attached to the data type declaration mentioned in the text – in this case, Duration. Our extension is also compatible with StandaloneDeriving, which is briefly discussed in Section 6.

To avoid clutter, we assume that all types have monomorphic kinds. However, it is easy to incorporate kind polymorphism [13], and our implementation of these ideas in GHC does so.

3.1 Well-Typed Uses of Deriving Via

Deriving Via grants the programmer the ability to put extra types in her programs, but the flip side to this is that it is possible for her to accidentally put total nonsense into a Deriving Via clause, such as:

```
newtype S = S Char
deriving Eq via Maybe
```

In this section, we describe a general algorithm for when a Deriving Via clause should typecheck, which will allow us to reject ill-formed examples like the one above.

3.1.1 Aligning Kinds

Suppose we are deriving the following instance:

```
data D d1 ... dm
    deriving (C c1 ... cn) via (V v1 ... vp)
```

In order for this declaration to typecheck, we must check the *kinds* of each type. In particular, the following conditions must hold:

The type C c₁ ... c_n must be of kind (k₁ -> ... -> k_r -> *) -> Constraint for some kinds k₁, ..., k_r. The reason is that the instance ⁴ we must generate,

instance C c₁ ... c_n (V v₁ ... v_p) => C c₁ ... c_n (D d₁ ... d_i) where ...

requires that we can apply $C c_1 \dots c_n$ to the types $\forall v_1 \dots v_p$ and $D d_1 \dots d_i$ (where i = m - r, see Section 3.1.2). Therefore, it would be nonsense to try to derive an instance of $C c_1 \dots c_n$ if it had kind, say, Constraint, since it couldn't be applied as above.

The kinds of ∨ v₁ ... v_p and D d₁ ... d_i, and the kind of the argument to C c₁ ... c_n must all unify. This check rules out the above example of deriving Eq via Maybe, as it does not even make sense to talk about reusing the Eq instance for Maybe—which is of kind (* -> *)—as Eq instances can only exist for types of kind *.

3.1.2 Shaping the Data Type

Note that in the conditions above, we specify $D d_1 \dots d_i$ (for some *i*), instead of $D d_1 \dots d_m$. That is because in general, the kind of the argument to $C c_1 \dots c_n$ is allowed to be different from the kind of $D d_1 \dots d_m$! For instance, the following example is perfectly legitimate:

```
class Functor (f :: * -> *) where ...
data Foo a = Foo a a
  deriving Functor
```

despite the fact that Foo a has kind * and the argument to Functor has kind ($* \rightarrow *$). This is because the code that actually gets generated has the following shape:

instance Functor Foo where ...

To put it differently, we have dropped the a in Foo a before applying Functor to it. The power to drop variables from the data type is part of what makes deriving clauses so flexible.

To determine how many variables to drop, we must examine the kind of $C c_1 \dots c_n$, which by condition (1) is of the form $((k_1 \rightarrow \dots \rightarrow k_r \rightarrow *) \rightarrow \text{Constraint})$ for some kinds k_1, \dots, k_r . Then the number of variables to drop is simply r, so to compute the i in $D d_1 \dots d_i$, we take i = m - r.

This is better explained by example, so consider the following two scenarios, both of which typecheck:

```
newtype A a = A a deriving Eq via (Identity a)
newtype B b = B b deriving Functor via Identity
```

In the first example, we have the class Eq, which is of kind * -> Constraint. The argument to Eq, which is of kind *, does not require that we drop any variables. As a result, we check that A a is of kind *, which is the case.

In the second example, we have the class Functor, which is of kind $(* \rightarrow *) \rightarrow$ Constraint. The argument to Functor is of kind $(* \rightarrow *)$, which requires that we drop one variable from B b to obtain B. We then check that B is kind of $(* \rightarrow *)$, which is true.

3.2 Code Generation

Once the typechecker has ascertained that a via type is fully compatible with the data type and the class for which an instance is being derived, GHC proceeds with generating the code for the instance itself. This generated code is then fed *back* into the typechecker, which acts as a final sanity check that GHC is doing the right thing under the hood.

3.2.1 Generalized Newtype Deriving (GND)

The process by which Deriving Via generates code is heavily based off of the approach that generalized newtype deriving (GND) takes, so it is informative to first explain how GND works. From there, Deriving Via is a straightforward generalization—so much so that Deriving Via can be thought of as "generalized GND".

Our running example in this section will be the newtype Age, which is a simple wrapper around Int (which we will call the *representation type*):

```
newtype Age = MkAge Int
    deriving Enum
```

⁴Technically, the context that is produced is not $C c_1 \dots c_n (\forall v_1 \dots v_p)$, but instead the residual constraints that are produced from GHC's constraint solver after simplifying that context. This is a property that Deriving Via shares with other forms of deriving as well.

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A naïve way to generate code would be to manually wrap and unwrap the MkAge constructor wherever necessary, such as in the code below:

```
instance Enum Age where
toEnum i = MkAge (toEnum i)
fromEnum (MkAge x) = fromEnum x
enumFrom (MkAge x) = map MkAge (enumFrom x)
```

This works, but is somewhat unsatisfying. After all, a newtype is intended to be a zero-cost abstraction that acts identically to its representation type at runtime. Accordingly, any function that mentions a newtype in its type signature should be able to be converted to a new function with all occurrences of the newtype in the type signature replaced with the representation type, and moreover, that new function should behave identically to the old one at runtime.

Unfortunately, the implementation of enumFrom may not uphold this guarantee. While wrapping and unwrapping the MkAge constructor is certain to be a no-op, the map function is definitely *not* a no-op, as it must walk the length of a list. But the fact that we need to call map in the first place feels rather silly, as all we are doing is wrapping a newtype at each element.

Luckily, there is a convenient solution to this problem: the safe coerce function [1]:

coerce :: Coercible a b => a -> b

Operationally, coerce can be thought of as behaving like its wily cousin, unsafeCoerce, which takes a value of one type as casts it to a value at a another type. Unlike unsafeCoerce, which can break programs if used carelessly, coerce is completely type-safe due to its use of the Coercible constraint. We explain Coercible in more detail in Section 3.2.2, but for now, it suffices to say that a Coercible a b constraint witnesses the fact that two types a and b have the same representation at runtime, and thus any value of type a can be safely cast to type b.

Armed with coerce, we can show what code GND would actually generate for the Enum Age instance above:

```
instance Enum Age where
```

```
toEnum =
   coerce @(Int -> Int) @(Int -> Age) toEnum
fromEnum =
   coerce @(Int -> Int) @(Age -> Int) fromEnum
enumFrom =
   coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Now we have a strong guarantee that the Enum instance for Age has exactly the same runtime characteristics as the instance for Int. As an added benefit, the code ends up being simpler as every method can be implemented as a straightforward application of coerce. The only interesting part is generating the two explicit type arguments [7] that are being used to specify the source type (using the representation type) and the target type (using the newtype) of coerce.

3.2.2 The Coercible Constraint

A Coercible constraint can be thought of as evidence that GHC can use to cast between two types. Coercible is not a type class, so it is impossible to write a Coercible instance by hand. Instead, GHC can generate and solve Coercible constraints automatically as part of its built-in constraint solver, much like it can solve equality constraints. (Indeed, Coercible can be thought of as a broader notion of equality among types.)

As mentioned in the previous section, a newtype can be safely cast to and from its representation type, so GHC treats them as inter-Coercible. Continuing our earlier example, this would mean that GHC would be able to conclude that:

```
instance Coercible Age Int
instance Coercible Int Age
```

But this is not all that Coercible is capable of. A key property is that GHC's constraint solver can look inside other type constructors when determining whether two types are inter-Coercible. For instance, both of these statements hold:

```
instance Coercible (Age -> [Age]) (Int -> [Int])
instance Coercible (Int -> [Int]) (Age -> [Age])
```

This demonstrates the ability to cast through the function and list type constructors. This ability is important, as our derived enumFrom instance would not typecheck otherwise!

Another crucial fact about Coercible that we rely on is that it is transitive: if Coercible a b and Coercible b c hold, then Coercible a c also holds. This is perhaps unsurprising if one views Coercible as an equivalence relation, but it is a fact that is worth highlighting, as the transitivity of Coercible is what allows us to coerce between newtypes. For instance, if we have these two newtypes:

```
newtype A a = A [a]
newtype B = B [Int]
```

then GHC is able to conclude that Coercible (A Int) B holds, because we have the following Coercible rules

```
instance Coercible (A Int) [Int]
instance Coercible [Int] B
```

as well as transitivity. As we will discuss momentarily, Deriving Via in particular makes heavy use of the transitivity of Coercible.

3.2.3 From GND to Deriving Via

As we saw in Section 3.2.1, the code which GND generates relies on coerce to do the heavy lifting. In this section, we generalize this technique slightly to give us a way to generate code for Deriving Via.

Recall the following GND-derived instance:

```
newtype Age = MkAge Int deriving Enum
```

As stated above, it generates the following code for enumFrom:

```
instance Enum Age where
...
enumFrom =
    coerce @(Int -> [Int]) @(Age -> [Age]) enumFrom
```

Here, there are two crucially important types: the representation type, Int, and the original newtype itself, Age. The implementation of enumFrom simply sets up an invocation of coerce enumFrom, with explicit type arguments to indicate that we should reuse the existing enumFrom implementation for Int and reappropriate it for Age.

The only difference in the code that GND and Deriving Via generate is that in the former strategy, GHC always picks the representation type for you, but in Deriving Via, the *user* has the power to choose this type. For example, if a programmer had written this instead:

```
newtype T = T Int
instance Enum T where ...
newtype Age = MkAge Int deriving Enum via T
```

then the following code would be generated:

enumFrom =
 coerce @(T -> [T]) @(Age -> [Age]) enumFrom

This time, GHC coerces from an enumFrom implementation for T (the via type) to an implementation for Age. (Recall from Section 3.2.2 that this is possible since we can coerce transitively from T to Int to Age).

Now we can see why the instances that Deriving Via can generate are a strict superset of those that GND can generate. For instance, our earlier GND example

newtype Age = MkAge Int deriving Enum

could equivalently have been written using Deriving Via like so:

newtype Age = MkAge Int deriving Enum via Int

Unlike GND, which is only suitable for deriving instances for newtypes, Deriving Via can derive instances for data types and newtypes alike (see Weekday in Section 2.2 for one example of a data type).

3.3 Type Variable Scoping

In the remainder of this section, we present an overview of how type variables are bound in Deriving Via clauses, and over what types they scope. Deriving Via introduces a new place where types can go, and more importantly, it introduces a new place where type variables can be *quantified*, so it takes some amount of care to devise a consistent treatment for it.

3.3.1 Binding Sites

Consider the following example:

data Foo a = ...
 deriving (Baz a b c) via (Bar a b)

Where is each type variable quantified?

- a is bound by Foo itself in the declaration data Foo a. Such a variable scopes over both the derived class, Baz a b c, as well as the via type, Bar a b.
- b is bound by the via type, Bar a b. Note that b is bound here but a is not, as it was bound earlier by the data declaration. b scopes over the derived class type, Baz a b c, as well.
- c is bound by the derived class, Baz a b c, as it was not bound elsewhere. (a and b were bound earlier.)

In other words, the order of scoping starts at the data declaration, then the via type, and then the derived classes associated with that via type.

3.3.2 Establishing Order

This scoping order may seem somewhat surprising, as one might expect the type variables bound by the derived classes to scope over the via type instead. However, this choice introduces additional complications that are tricky to resolve. For instance, consider a scenario where one attempts to derive multiple classes at once with a single via type:

data D

deriving (C1 a, C2 a) via (T a)

Suppose we first quantified the variables in the derived classes and made them scope over the via type. Because each derived class has its own type variable scope, the a in C1 a would be bound independently from the a in C2 a. In other words, we would have something like this (using a hypothetical forall syntax):

```
deriving (forall a . C1 a, forall a . C2 a) via (T a)
```

Now we are faced with a thorny question: which a is used in the via type, \top a? There are multiple choices here, since the a variables in C1 a and C2 a are distinct! This is an important decision, since the kinds of C1 and C2 might differ, so the choice of a could affect whether \top a kind-checks or not.

On the other hand, if one binds the a in \top a first and has it scope over the derived classes, then this becomes a non-issue. We would instead have this:

deriving (C1 a, C2 a) via (forall a . T a)

Now, there is no ambiguity regarding a, as both a variables in the list of derived classes were bound in the same place.

It might feel strange visually to see a variable being used *before* its binding site (assuming one reads code from left to right). However, this is not unprecedented within Haskell, as this is also legal:

f = g + h where g = 1; h = 2

In this example, we have another scenario where things are bound (g and h) after their use sites. In this sense, the via keyword is continuing a rich tradition pioneered by where clauses.

One alternative idea (which was briefly considered) was to put the via type *before* the derived classes so as to avoid this "zigzagging" scoping. However, this would introduce additional ambiguities. Imagine one were to take the example

deriving Z via X Y

and convert it to a form in which the via type came first:

deriving via X Y Z

Should this be parsed as (X Y) Z, or X (Y Z)? It's not clear visually, so this choice would force programmers to write additional parentheses.

4 More Use Cases

We have already seen in Section 2 how Deriving Via facilitates greater code reuse in the context of QuickCheck. This is far from the only domain where Deriving Via proves to be a natural fit, however. In fact, there are so many of these domains, there would be enough to fill pages upon pages!

Unfortunately, we do not have enough space to document all of these use cases, so in this section, we present a crosssection of scenarios in which Deriving Via can capture interesting patterns and allow programmers to abstract over them in a convenient way.

4.1 Asymptotic Improvements with Ease

A widely used feature of type classes is their ability to give default implementations for their methods if a programmer leaves them off. One example of this can be found in the Applicative class. The main workhorse of Applicative is the (<*>) method, but on occasion, it is more convenient to use the (<*) or (*>) methods, which sequence their actions but discard the result of one of their arguments:

```
class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
  (<*) :: f a -> f b -> f a
  (<*) = liftA2 (\ a _ -> a)
  (*>) :: f a -> f b -> f b
  (*>) = liftA2 (\ _ b -> b)
```

As shown here, (<*) and (*>) have default implementations in terms of liftA2. This works for any Applicative, but is not as efficient as it could be in some cases. For some instances of Applicative, we can actually implement these methods in O(1) time instead of using liftA2, which can often run in superlinear time. One such Applicative is the function type (->):

```
instance Applicative ((->) r) where
    pure = const
    (<*>) f g x = f x (g x)
    f <* _ = f
    _ *> g = g
```

Note that we had to explicitly define (<*) and (*>), as the default implementations would not have been as efficient.

But (->) is not the only type for which this trick works it also works for any data type that is isomorphic to (->) r (for some r). These function-like types are characterized by the Representable type class:

class Functor f => Representable f where
 type Rep f
 index :: f a -> (Rep f -> a)
 tabulate :: (Rep f -> a) -> f a

This is a good deal more abstract than (->) r, so it can be helpful to see how Representable works for (->) r itself:

instance Representable ((->) r) where
type Rep ((->) r) = r
index f = f
tabulate f = f

With Representable, we can codify the Applicative shortcut for (<*) and (*>) with a suitable newtype:

```
newtype WrapRep f a = WrapRep (f a)
deriving (Functor, Representable)
instance Representable f
  => Applicative (WrapRep f) where
  pure = tabulate . pure
  f <*> g = tabulate (index f <*> index g)
  f <* _ = f
  _ *> g = g
```

Now, instead of having to manually override (<*) and (*>) to get the desired performance, one can accomplish this in a more straightforward fashion by using Deriving Via:

```
newtype IntConsumer a = IntConsumer (Int -> a)
deriving (Functor, Representable)
deriving Applicative via (WrapRep IntConsumer)
```

Not only does this save code in the long run, but it also gives a name to the optimization being used, which allows it to be documented, exported from a library, and thereby easier to spot "in the wild" for other programmers.

4.2 Making Defaults more Flexible

In the previous section, we saw an example of how relying too much on a type class's default implementations can backfire. This is an unfortunately common trend with type classes in general: many classes try to pick one-size-fits-all defaults that do not work well in certain scenarios, but because Haskell allows specifying only one default per method, if the provided default does not work for a programmer's use case, then she is forced to write her own implementations by hand.

In this section, we continue the trend of generalizing defaults by looking at another language extension that Deriving Via can substitute for: *default signatures*. Default signatures (a slight generalization of default implementations) can eliminate large classes of boilerplate, but they too are limited by the one-default-per-method restriction. Here, we demonstrate how one can scrap uses of default signatures in favor of Deriving Via and show how Deriving Via can overcome the limitations of default signatures.

The typical use case for default signatures is when one has a class method that has a frequently used default implementation at a constrained type. For instance, consider a Pretty class with a method pPrint for pretty-printing data:

```
class Pretty a where
    pPrint :: a -> Doc
```

Coming up with Pretty instances for the vast majority of data types is repetitive and tedious, so a common pattern is to abstract away this tedium using generic programming libraries, such as those found in GHC.Generics [11] or generics-sop [4]. For example, using GHC.Generics, we can define

```
genericPPrint ::
```

(Generic a, GPretty (Rep a)) => a -> Doc

The details of how Generic, GPretty, and Rep work are not important to understanding the example. What is important is to note that we cannot just add

```
pPrint = genericPPrint
```

as a conventional default implementation to the Pretty class, because it does not typecheck due to the extra constraints.

Before the advent of default signatures, one had to work around this by defining pPrint to be genericPPrint in every Pretty instance, as in the examples below:

```
instance Pretty Bool where
   pPrint = genericPPrint
instance Pretty a => Pretty (Maybe a) where
   pPrint = genericPPrint
```

To avoid this repetition, default signatures allow one to provide a default implementation of a class method using *additional* constraints on the method's type. For example:

```
class Pretty a where
  pPrint :: a -> Doc
  default pPrint ::
    (Generic a, GPretty (Rep a)) => a -> Doc
  pPrint = genericPPrint
```

Now, if any instances of Pretty are given without an explicit definition of pPrint, the default implementation is used. For this to typecheck, the data type a used in the instance must satisfy the constraints (Generic a, GPretty (Rep a)). Thus, we can reduce the instances above to just

```
instance Pretty Bool
instance Pretty a => Pretty (Maybe a)
```

Although default signatures remove the need for many occurrences of boilerplate code, it also retains a significant limitation of Haskell default methods: every class method can have at most one default implementation. As a result, default signatures effectively endorse one default implementation as the canonical one. But in many scenarios, there is far more than just one way to do something. Our pPrint example is no exception. Instead of genericPPrint, one might want to:

- leverage a Show-based default implementation instead of a Generic-based one,
- use a different generic programming library, such as generics-sop, instead of GHC.Generics, or
- use a tweaked version of genericPPrint that displays extra debugging information.

All of these are perfectly reasonable choices a programmer might want to make, but alas, GHC lets type classes bless each method with only one default.

Fortunately, Deriving Via provides a convenient way of encoding default implementations with the ability to toggle between different choices: newtypes! For instance, we can codify two different approaches to implementing pPrint as follows:

```
newtype GenericPPrint a = GenericPPrint a
instance (Generic a, GPretty (Rep a))
=> Pretty (GenericPPrint a) where
pPrint (GenericPPrint x) = genericPPrint x
```

newtype ShowPPrint a = ShowPPrint a

instance Show a => Pretty (ShowPPrint a) where
 pPrint (ShowPPrint x) = stringToDoc (show x)

With these newtypes in hand, choosing between them is as simple as changing a single type:

```
deriving Pretty via (GenericPPrint DataType1)
deriving Pretty via (ShowPPrint DataType2)
```

We have seen how Deriving Via makes it quite simple to give names to particular defaults, and how toggling between defaults is a matter of choosing a name. In light of this, we believe that many current uses of default signatures ought to be removed entirely and replaced with the Deriving Viabased idiom presented in this section. This avoids the need to bless one particular default and forces programmers to consider which default is best suited to their use case, instead of blindly trusting the type class's blessed default to always do the right thing.

An additional advantage is that it allows decoupling the definition of such defaults from the site of the class definition. Hence, if a package author is hesitant to add a default because that might incur an unwanted additional dependency, nothing is lost, and the default can simply be added in a separate package.

4.3 Deriving via Isomorphisms

All of the examples presented thus far in the paper rely on deriving through data types that have the same runtime representation as the original data type. In the following, however, we point out that—perhaps surprisingly—we can also derive through data types that are *isomorphic*, not just representationally equal. To accomplish this feat, we rely on techniques from generic programming.

Let us go back to QuickCheck (as in Section 2) once more and consider the data type

data Track = Track Title Duration

for which we would like to define an Arbitrary instance. Let us further assume that we already have Arbitrary instances for both Title and Duration.

The QuickCheck library defines an instance for pairs, so we could generate values of type (Title, Duration), and in essence, this is exactly what we want. But unfortunately, the two types are not inter-Coercible, even though they are isomorphic⁵.

However, we can exploit the isomorphism and still get an instance for free, and the technique we apply is quite widely applicable in similar situations. As a first step, we declare a newtype to capture that one type is isomorphic to another:

```
newtype SameRepAs a b = SameRepAs a
```

We call this type SameRepAs, because it denotes that a and b have inter-Coercible generic representations, i.e., that

Coercible (Rep a ()) (Rep b ())

holds. Furthermore, the type SameRepAs a b is representationally equal to a, which implies that a and SameRepAs a b are inter-Coercible.

We now witness the isomorphism between the two types via their generic representations: if they have inter-Coercible generic representations, we can transform back and forth between the two types using the from and to methods of the Generic class from GHC. Generics [11]. We can use this to define a suitable Arbitrary instance for SameRepAs:

```
instance
```

```
( Generic a, Generic b
, Coercible (Rep a ()) (Rep b ()), Arbitrary b
) => Arbitrary (a 'SameRepAs' b) where
arbitrary = SameRepAs . coerceViaRep <$> arbitrary
where
    coerceViaRep :: b -> a
    coerceViaRep =
        to . (coerce :: Rep b () -> Rep a ()) . from
```

Here, we first use arbitrary to give us a generator of type Gen b, then coerce this via the generic representations into an arbitrary value of type Gen a.

Finally, we can use the following deriving declarations for Track to obtain the desired Arbitrary instance:

```
deriving Generic
deriving Arbitrary
via (Track 'SameRepAs' (String, Duration))
```

With this technique, we can significantly expand the "equivalence classes" of data types that can be used when picking suitable types to derive through.

4.4 Retrofitting Superclasses

On occasion, the need arises to retrofit an existing type class with a superclass, such as when Monad was changed to have Applicative as a superclass (which in turn has Functor as a superclass).

One disadvantage of such a change is that if the primary goal is to define the Monad instance for a type, one now has to write two additional instances, for Functor and Applicative, even though these instances are actually determined by the Monad instance.

With Deriving Via, we can capture this fact as a newtype, thereby making the process of defining such instances much less tedious:

```
newtype FromMonad m a = FromMonad (m a)
  deriving Monad
instance Monad m => Functor (FromMonad m) where
  fmap = liftM
instance Monad m => Applicative (FromMonad m) where
  pure = return
  (<*>) = ap
```

Now, if we have a data type with a Monad instance, we can simply derive the corresponding Functor and Applicative instances by referring to FromMonad:

```
data Stream a b = Done b | Yield a (Stream a b)
  deriving (Functor, Applicative)
   via (FromMonad (Stream a))
instance Monad (Stream a) where
  return = Done
  Yield a k ≫= f = Yield a (k ≫= f)
  Done b ≫= f = f b
```

One potentially problematic aspect remains. Another proposal [12] has been put forth (but has not been implemented, as of now) to remove the return method from the Monad class and make it a synonym for pure from Applicative. The argument is that return is redundant, given that pure does the same thing with a more general type signature. All other prior discussion about the proposal aside, it should be noted that removing return from the Monad class would prevent FromMonad from working, as then Monad instances would not have any way to define pure. ⁶

4.5 Avoiding Orphan Instances

Not only can Deriving Via quickly procure class instances, in some cases, it can eliminate the need for certain instances

⁵Isomorphic in the sense that we can define a function from Track to (Title, Duration) and vice versa. Depending on the class we want to derive, sometimes an even weaker relationship between the types is sufficient, but we focus on the case of isomorphism here for reasons of space.

⁶A similar, yet somewhat weaker, argument applies to suggested changes to relax the constraints of liftM and ap to merely Applicative and to change their definitions to be identical to fmap and (<*>), respectively.

altogether. Haskell programmers often want to avoid *orphan instances*: instances defined in a separate module from both the type class and data types being used. Sometimes, however, it is quite tempting to reach for orphan instances, as in the following example adapted from a blog post by Gonzalez [10]:

```
newtype Plugin = Plugin (IO (String -> IO ()))
deriving Semigroup
```

In order for this derived Semigroup instance to typecheck, there must be a Semigroup instance for IO available. Suppose for a moment that there was no such instance for IO. How could one work around this issue?

- One could patch the base library to add the instance for IO. But given base's slow release cycle, it would be a while before one could actually use this instance.
- Write an orphan instance for I0. This works, but is undesirable, as now anyone who uses Plugin must incur a possibly unwanted orphan instance.

Luckily, Deriving Via presents a more convenient third option: re-use a Semigroup instance from *another* data type. Recall the Ap data type from Section 1.2 that lets us define a Semigroup instance by lifting through an Applicative instance. As luck would have it, IO already has an Applicative instance, so we can derive the desired Semigroup instance for Plugin like so:

newtype Plugin = Plugin (IO (String -> IO ()))
deriving Semigroup
via (Ap IO (String -> Ap IO ()))

Note that we have to use Ap twice in the via type, corresponding to the two occurences of IO in the Plugin type. This is possible because Ap IO has the same representation as IO, and it is also necessary if we want to completely bypass the need for a Semigroup instance for IO: Via the inner Ap IO () and the existing instance

instance Semigroup b => Semigroup (a -> b)

we first obtain a Semigroup instance for String \rightarrow IO (), which we then, via the outer Ap IO application, lift to IO (String \rightarrow IO ()) and therefore the Plugin type.

5 Related Ideas

We have demonstrated in the previous section that Deriving Via is an extremely versatile technique, and can be used to tackle a wide variety of problems. Deriving Via also bears a resemblance to other distinct language features which address similar issues, so in this section, we present an overview of their similarities and differences.

5.1 Code Reuse in Dependent Type Theory

Diehl *et al.* present a dependent type theory which permits zero-cost conversions between indexed and non-indexed variants of data types [5], much in the same vein as Coercible.

However, these conversions must be explicitly constructed with combinators, whereas Coercible-based casts are built automatically by GHC's constraint solver. Therefore, while Diehl *et al.* allow conversions between more data types than Deriving Via does, it also introduces some amount of boilerplate than Deriving Via avoids.

5.2 Explicit Dictionary Passing

The power and flexibility of Deriving Via is largely due to GHC's ability to take a class method of a particular type and massage it into a method of a different type. This process is almost completely abstracted away from the user, however. A user only needs to specify the types involved, and GHC will handle the rest behind the scenes.

An alternative approach, which would put more power into the hands of the programmer, is to permit the ability to explicitly construct and pass the normally implicit dictionary arguments corresponding to type class instances [6]. Unlike in Deriving Via, where going between class instances is a process that is carefully guided by the compiler, permitting explicit dictionary arguments would allow users to actually coerce concrete instance values and pass them around as first-class values. In this sense, explicit dictionary arguments could be thought of as a further generalization of the technique that Deriving Via uses.

However, explicit dictionary arguments are a considerable extension of the language and its type system, and we feel that to be too large a hammer for the nail we are trying to hit. Deriving Via works by means of a simple desugaring of code with some light typechecking on top, which makes it much simpler to describe and implement. Finally, the problem that explicit dictionaries aim to solve—resolving ambiguity in implicit arguments—almost never arises in Deriving Via, as the programmer must specify all the types involved in the process.

6 Current Status

We have implemented Deriving Via within GHC. Our implementation also interacts well with other GHC features that were not covered in this paper, such as kind polymorphism [13], StandaloneDeriving, and type classes with associated type families [2]. However, there are still challenges remaining, which we describe in this section.

6.1 Quality of Error Messages

The nice thing about deriving is that when it works, it tends to work extremely well. When it *doesn't* work, however, it can be challenging to formulate an error message that adequately explains what went wrong. The fundamental issue is that error messages resulting from uses of deriving are usually rooted in *generated* code, and pointing to code that the user did not write in error messages can lead to a confusing debugging experience. Haskell '18, September 27-28, 2018, St. Louis, MO, USA

Fortunately, we have found in our experience that the quality of Deriving Via-related error messages is overall on the positive side. GHC has already invested significant effort into making type errors involving Coercible to be easily digestible by programmers, so Deriving Via benefits from this work. For instance, if one inadvertently tries to derive through a type that is not inter-Coercible with the original data type, such as in the following example:

```
newtype UhOh = UhOh Char deriving Ord via Int
```

Then GHC will tell you exactly that, in plain language:

 Couldn't match representation of type Char with that of Int arising from the coercion of the method compare from type 'Int -> Int -> Ordering' to type 'UhOh -> UhOh -> Ordering'

That is not to say that every error message is this straightforward. There are some scenarios that produce less-thanideal errors, such as this:

newtype Foo a = Foo (Maybe a) deriving Ord via a

 Occurs check: cannot construct the infinite type: a ~ Maybe a arising from the coercion of the method 'compare' from type 'a -> a -> Ordering' to type 'Foo a -> Foo a -> Ordering'

The real problem is that a and Maybe a do not have the same representation at runtime, but the error does not make this obvious. It is possible that one could add an *ad hoc* check for this class of programs, but there are likely many more tricky corner cases lurking around the corner given that one can put anything after via.

We do not propose a solution to this problem here, but instead note that issues with Deriving Via error quality are ultimately issues with coerce error quality, given that the error messages are a result of coerce failing to typecheck. It is likely that investing more effort into making coerce's error messages easier to understand would benefit Deriving Via as well.

6.2 Multi-Parameter Type Classes

GHC extends Haskell by permitting type classes with more than one parameter. Multi-parameter type classes are extremely common in modern Haskell, to the point where we assumed the existence of them in Section 3.1.1 without further mention. However, multi-parameter type classes pose an intriguing design question when combined with Deriving Via and StandaloneDeriving, another GHC feature that allows one to write deriving declarations independently of a data type.

For example, one can write the following instance using StandaloneDeriving:

```
class Triple a b c where
  triple :: (a, b, c)
```

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```
instance Triple () () () where
  triple = ((), (), ())
newtype A = A ()
newtype B = B ()
newtype C = C ()
deriving via () instance Triple A B C
```

However, the code this generates is somewhat surprising. Instead of reusing the Triple () () () instance in the derived instance, GHC will attempt to reuse an instance for the type Triple A B (). The reason is that, by convention, StandaloneDeriving will only ever coerce through the *last* argument of a class. That is because the standalone instance above would be the same as if a user had written:

```
newtype C = C () deriving (Triple A B) via ()
```

This consistency is perhaps a bit limiting in this context, where we have multiple arguments to C that one could "derive through". But it is not clear how GHC would figure out which of these arguments to C should be derived through, as there seven different combinations to choose from! It is possible that another syntax would need to be devised to allow users to specify which arguments should be coerced to avoid this ambiguity.

7 Conclusions

In this paper, we have introduced the Deriving Via language extension, explained how it is implemented, and shown a wide variety of use cases. We believe that Deriving Via has the potential to dramatically change the way we write instances, as it encourages giving names to recurring patterns and reusing them where needed. It is our feeling that most instance declarations that occur in the wild can actually be derived by using a pattern that deserves to be known and named, and that instances defined manually should become an anti-pattern in all but some rare situations.

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